

# Combustion of liquid fuel inside inert porous media: an analytical approach

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## Abstract

This paper presents a numerical analysis of combustion of liquid fuel droplets suspended in air inside an inert porous media. A one-dimensional heat transfer model has been developed assuming complete vaporization of oil droplets prior to their entry into the flame. The effects of absorption coefficient, emissivity of medium, flame position on radiative energy output efficiency and optimum oil droplet size at the entry, defined as the maximum size for complete vaporization before entering the combustion zone, have been presented. The inert porous medium with low absorption coefficient will produce high downstream radiative output with large oil droplet sizes.

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## 1. Introduction

In the last few decades, porous media burners of gaseous fuel have shown lot of promise over the conventional burners. The premixed gaseous fuel–air mixture is burnt inside the solid porous matrix to release the heat of combustion to heat up the matrix which converts sensible heat of combustion to radiative energy. The radiative energy not only preheats the reactant gas mixture in the upstream section for combustion augmentation but also emits radiation in the downstream end to heat the load. The advantages of porous media burners are high power density, very low emission, very wide power range, combustion stability over wide range of equivalence ratio and high thermal efficiency. These advantages

of porous radiative burners have led to their various thermal applications [1,2].

Many combustion models have been developed [3–6] to analyze the combustion characteristics of porous media burner for premixed gaseous fuel–air system. But for combustion of liquid fuel using porous media, only a few experimental and theoretical studies have been reported. Takami et al. [7] studied the combustion behavior of kerosene when the fuel was added drop wise at the top of the porous ceramic plate and ignited at the bottom surface of the plate. Jugjai and Polmart [8] used a set up containing porous ceramic media and packed bed with air mixing chamber in between them. Kerosene was added drop wise to the top of ceramic matrix. Kerosene got vaporized while traveling through porous matrix and met the swirling air in combustion chamber and finally the packed bed was used in the downstream section to convert thermal energy to radiation energy for emission. Temperature profile for both axial and radial position of the set up was measured and analyzed. Fuse et al. [9] used the radiant energy of kerosene flame and

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**Nomenclature**

$a$	specific area, $m^{-1}$	$Sh$	Sherwood number
$A$	pre-exponential factor in reaction rate, $s^{-1}$	$T$	temperature, K
$Bi$	Biot number	$T_A$	autoignition temperature, K
$c$	specific heat of gas at constant pressure, $Jkg^{-1}K^{-1}$	$\bar{T}$	average film temperature, $(T_g + T_i)/2$
$c_{pv}$	specific heat of oil vapor at constant pressure, $Jkg^{-1}K^{-1}$	$T^*$	dimensionless gas temperature, $(T_g - T_i)/T_i$
$d$	Sauter mean diameter of oil droplet, $\mu m$	$T^{*'}_1$	dimensionless peak gas temperature, $(T_m - T_i)/T_i$
$d^*$	optimum Sauter mean diameter of oil droplet, $\mu m$	$u$	axial velocity, $ms^{-1}$
$d'$	dimensionless diameter of oil droplet, $dd^*$	$u_L$	laminar burning velocity of stoichiometric oil–air mixture, $ms^{-1}$
$D$	diffusion coefficient, $m^2s^{-1}$	$V^*$	dimensionless burning velocity, $u_3/u_L$
$E$	activation energy, $Jkgmol^{-1}$	$x$	axial coordinate, m
$E^*$	emissivity of solid	$x'$	value of $x$ where $T^* = 0.01$
$E'$	downstream radiative efficiency in percent, $q^*(L)/q'$	$x''$	value of $x$ where $p_{vo}/p = 0.01$
$E''$	total radiative efficiency in percent, $[q^*(L) - q^*(0)]/q'$	$x^*$	axial coordinate at flame plane, m
$h$	heat transfer coefficient, $Wm^{-2}K^{-1}$	$X$	dimensionless axial coordinate, $x/L$
$i$	radiation intensity, $Wm^{-2}$	$X^*$	dimensionless axial coordinate at flame plane, $x^*/L$
$i_b$	black body intensity, $Wm^{-2}$	$y$	mass fraction of gaseous product
$k$	thermal conductivity, $Wm^{-1}K^{-1}$	$Y$	constant as in Eq. (6)
$L$	porous layer length, m	<i>Greek symbols</i>	
$L^*$	optical thickness, $\alpha L$	$\alpha$	absorption coefficient, $m^{-1}$
$L'$	dimensionless preheating temperature zone length, $(x^* - x')/L$	$\varphi$	porosity
$L''$	dimensionless effective oil vaporization length, $(x^* - x'')/L$	$\rho$	density, $kgm^{-3}$
$m$	mass of single liquid droplet, kg	$\sigma$	Stefan–Boltzman constant, $Wm^{-2}T^{-4}$
$M$	average molecular weight, $kgmol^{-1}$	$\psi$	inertial impaction factor
$M_1, M_2, M_3$	dimensionless quantities as in Eq. (17)	$\lambda$	latent heat of vaporization of oil, $Jkg^{-1}$
$n$	number density of droplets, $m^{-3}$	<i>Superscripts</i>	
$n_f$	fuel concentration, $kgmolm^{-3}$	+	forward direction
$n_{O_2}$	oxygen concentration, $kgmolm^{-3}$	–	backward direction
$Nu$	Nusselt number	<i>Subscripts</i>	
$p$	pressure, $Nm^{-2}$	b	boiling point of liquid
$p_v$	partial vapor pressure, $Nm^{-2}$	e	exit plane
$q$	radiative heat flux, $Wm^{-2}$	f	flame plane
$q^*$	net radiative heat flux, $Wm^{-2}$	g	gas
$q'$	reaction enthalpy flux, $Wm^{-2}$	gl	between gas and liquid
$Q$	dimensionless radiative heat flux, $q/(\sigma T_i^4)$	gs	between gas and solid
$Q^*$	dimensionless net radiative heat flux, $q^*/(\sigma T_i^4)$	i	inlet
$Q'$	dimensionless reaction enthalpy flux, $q'/(\sigma T_i^4)$	l	liquid
$R$	Universal gas constant, $Jkgmol^{-1}K^{-1}$	m	maximum
$Re$	Reynolds number	o	droplet surface
$s$	scattering coefficient, $m^{-1}$	s	solid
$Sc$	Schmidt number	v	vapor
		$\infty$	bulk gas
		1, 2, 3, 4	interfacial planes

furnace walls for penetration through porous ceramic plate to vaporize the oil from the oil container for con-

tinuous oil vaporization and sustenance of stable combustion. Premixed fuel oil sprayed droplets in air were

used in place of gaseous fuel–air mixture for porous radiant burner using ceramic matrix by several investigators [10,11]. They got stabilized combustion inside the matrix and studied effect of various parameters on the combustion inside the matrix. Martynenko et al. [12] formulated a mathematical model where the oil droplets vaporize inside an inert porous medium with self-sustained combustion of the oil vapor–air mixture. The model considers the behavior of oil droplets which collide and deposit on the porous solid structure and also their effect on heat transfer parameters. Tseng and Howell [13] have conducted both experimental and numerical studies of liquid heptane droplet vaporization and combustion of gaseous mixture inside the inert porous medium made of zirconia. The flashback and blow-off limits of the combustion within the porous structure were determined. It was concluded that smaller droplet size ( $<25\mu\text{m}$ ) of heptane could be evaporated in the low temperature region before the flame front.

The present study investigates the thermal behavior of a highly porous ceramic matrix for combustion of premixed sprayed kerosene droplets in air where the liquid droplets are completely vaporized in the low temperature region just before reaching the flame front.

## 2. Mathematical analysis

### 2.1. Analytical model

The schematic diagram representing the one-dimensional model under steady state condition is shown in Fig. 1. A mixture of sprayed oil (kerosene) droplets in laminar flow enters an adiabatic duct containing inert porous medium of total length  $L$ . The oil–air mixture enters medium ( $x = 0$ ) at temperature  $T_i$ . The combustion gas finally leaves the medium through region C at  $x = L$  at temperature  $T_e$ . The porous medium is divided

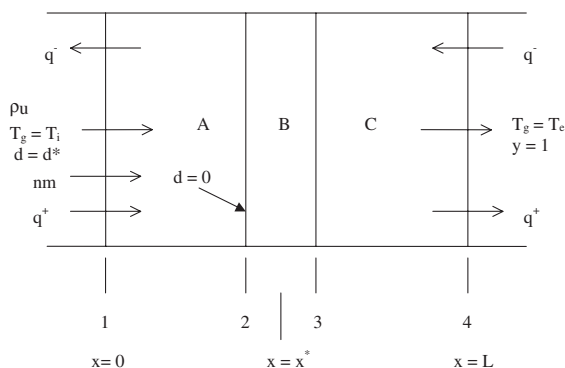


Fig. 1. Schematic diagram of combustion system in a porous medium.

into three regions A, B and C. The interfacial planes (1, 2, 3 and 4) are perpendicular to  $x$ -direction and separating the regions. The radiative heat fluxes in forward and backward directions in the porous medium are  $q^+$  and  $q^-$  respectively.

The principal assumptions used in the formulation are as follows:

- The working gas is non-radiating.
- The structure is having high porosity and the gas flow is laminar so that the pressure drop across the porous medium is negligible.
- The porous medium is a homogeneous continuum, the physical properties of which are given by multiplying those of porous material by a factor of  $(1 - \phi)$ .
- The porous medium is able to emit and absorb radiation in local thermal equilibrium while radiative scattering is ignored.
- A one-dimensional radiative propagation occurs in  $x$ -direction without any reaction being taken place in regions A and C.
- The size of inlet oil droplets ( $d^*$ ) is optimum such that the vaporization of oil droplets is complete just before entering the combustion region B.
- Velocities of air and liquid droplets are same in region A.
- No temperature gradient exists inside each droplet.
- Physical interaction occurring between porous medium surface and oil droplets suspended in air is negligible.

The assumptions in the region B for the reaction system are:

- The porous medium is non-catalytic.
- The oil vapor–air mixture enters the region at a temperature  $T_g \leq T_A$  where  $T_A$  is the autoignition temperature of oil vapor–air mixture.
- The reaction starts and gets completed in the region at constant temperature  $T_g = T_m$ .
- The medium at interface 2 absorbs radiation as upward radiation flux in region A.
- The one-step global irreversible reaction between oil vapor and air is considered.

Some of these assumptions are discussed in details. The assumption (a) is realized as the emissivity of the gas is much less than the porous solid medium. The assumption (b) is justified as the usual matrix structure of radiant burners [6] is in the form of ceramic porous open cellular foams or ceramic fibre structure which has very high porosity in the range of 0.95–0.99. Also low pressure drop across the porous solid is justified due to laminar flow of gas through highly porous solid

medium. The assumption (d) is realized to cover most of the porous medium such as ceramic foam [5] and porous metallic media [3]. The assumption (e) is reasonable due to good thermal insulation outside the duct in presence of negligible radial flow.

The assumptions (f)–(i) need discussions in details. In this study, fine oil droplets ( $d < 14\mu$ ), which are generated usually in air atomizing nozzles [14] in a separate container, enter the porous media so that each droplet gets sufficient time to reach its terminal velocity which is very small in comparison to bulk velocity of air so that the velocity of each droplet is nearly equal to that of air velocity. For such fine droplets, Biot number  $[hd/k]$  is estimated to be much less than 0.1 so that no temperature gradient can exist within each droplet [15]. For ceramic foam with low pore density (number of pores per inch), the collecting structure [9,16] for aerosol of oil in air is assumed to be cylindrical of average diameter 1.5 mm. Inertial impaction factor ( $\psi$ ) based on Stokes law for cylindrical target on the flow of aerosol path relevant to the present study has been estimated [17]. The maximum value of  $\psi^{1/2}$  is nearly 0.4 which corresponds to inertial impact efficiency of 0.03. With this low collection efficiency of porous structure, the physical interaction of aerosol with porous solid structure is assumed to be insignificant.

The assumptions (k)–(n) are discussed in totality. As the porosity of the solid medium is very high ( $\phi > 0.9$ ) and the gas mixture flow is laminar, the flow may be assumed to be of plug flow nature. In kerosene–air combustion [18], the one step global reaction rate is given by  $k_c = 5 \times 10^{11} \exp[-30,000/RT_g][n_f]^{0.25}[n_{O_2}]^{1.5} \text{ gmol cm}^{-3} \text{ s}^{-1}$  when  $n_f$  and  $n_{O_2}$  are fuel and oxygen concentration respectively using kerosene ( $C_{12}H_{24}$ ). With peak reaction temperature of this system assumed at 2000 K and 99% completion of reaction under the plug flow condition, the reaction thickness is estimated to be about a fraction of millimeter. This dimension is smaller or nearly equal to the dimension of cavity for highly porous ceramic [5] or metallic structure [4]. With high permeability and porosity of matrix structure, the combustion can be realized as if in open space flow condition in such a small thickness so that the assumption of constant temperature of reaction zone is justified as in assumption (l). The maximum temperature of the gas mixture before it enters the reaction region B is its autoignition temperature,  $T_A$ . However the inlet temperature at interface 2 is determined by the absorptivity of the porous medium facing reaction zone temperature,  $T_m$ . At steady state, the gas mixture at  $T_g \leq T_A$  when enters the reaction region instantaneously reaches the reaction temperature  $T_m$  because of high reaction enthalpy flux. For methane combustion in porous matrix, the gas entry temperature,  $T_2$  was obtained to be less than  $T_A$  [3]. So the assumption (m) is justified as the interface 2 exchanges radiative enthalpy from reaction region B only through emissive/

absorptive interaction between reaction temperature  $T_m$  and low solid temperature at 2. Other assumptions (j) and (n) are taken for computational simplicity.

## 2.2. Basic equations

Using above assumptions, the continuity equation for the species, energy equations for both gas, liquid and solid phases are formulated respectively [4,18,19].

In reaction region B,

$$\rho u(\partial y/\partial x) = D\rho(\partial^2 y/\partial x^2) + A\rho(1-y) \times \exp[-E/(RT_m)] \quad (1)$$

where mass production rate of species is in first order Arrhenius form.

In region A

$$\rho c(\partial T_g/\partial x) = k_g(\partial^2 T_g/\partial x^2) - h_{gl}(n\pi d^2)(T_g - T_1) - h_{gs}a_s(T_g - T_s) \quad (2)$$

$$-n\lambda u_l(\partial m/\partial x) = h_{gl}(n\pi d^2)(T_g - T_1) \quad (3)$$

Equation of state:

$$\rho = pM/(RT_g) \quad (4)$$

In region A, for high rate of vaporization of liquid drops at high gas temperature both mass and heat transfer coefficients are modified incorporating the effect of superheating vapor and bulk flow rate of vapor [18]. The vaporization rate of single liquid drop can be expressed as

$$-u_l(\partial m/\partial x) = \pi d D p / (RT) [\ln\{(p - p_{vz})/(p - p_{vo})\}] \times (2 + 0.6 Re^{1/2} Sc^{1/3}) \quad (5)$$

where  $\mathcal{F}$  = mean film temperature of liquid drop =  $(T_g + T_1)/2$ .

$T_1$  is estimated [18] using following equation

$$T_1 = T_g - (\lambda/c_{pv})(e^Y - 1) \quad (6)$$

where  $Y = [(c_{pv} D p)/(R \mathcal{F} k_g)] [Sh/Nu] [\ln\{p/(p - p_{vo})\}]$ .

In Eqs. (5) and (6), the values of  $D$ ,  $k_g$ ,  $c_{pv}$  are evaluated at  $\mathcal{F}$  and those of  $p_{vo}$  and  $\rho_1$  at  $T_1$ .

In the present case,  $u_l = u$ , i.e.  $Re_1 = 0$  and  $Sh = Nu = 2$ . Also for high mass ratios of air to fuel,  $p_{vz} \approx 0$  and Eq. (5) becomes

$$\partial(d^2)/\partial x = -[(8pD)/(RTu\rho_l)] [\ln\{p/(p - p_{vo})\}] \quad (7)$$

where  $m = \rho_l \pi d^3/6$ .

In region C

$$\rho c(\partial T_g/\partial x) = k_g(\partial^2 T_g/\partial x^2) - h_{gs}a_s(T_g - T_s) \quad (8)$$

In A and C regions, the net radiative heat flux,  $q^*$  is related to heat fluxes  $q^+$  and  $q^-$  in forward and backward directions as

$$q^* = q^+ - q^- \tag{9}$$

$$\partial q^* / \partial x = k_s (\partial^2 T_s / \partial x^2) + h_{gs} a_s (T_g - T_s) \tag{10}$$

Using two-flux gray radiation approximation [19], the equation of transfer for intensity in each hemisphere is integrated over their respective hemispheres to yield forward and backward intensities  $i^+$  and  $i^-$  as

$$\partial i^+ / (2\partial x) = -(\alpha + s) i^+ + s i^- + \alpha i_b \tag{11}$$

$$-\partial i^- / (2\partial x) = -(\alpha + s) i^- + s i^+ + \alpha i_b \tag{12}$$

where  $i_b$  is the black body intensity. As each intensity over their respective hemisphere is constant under the two-flux model, Eqs. (11) and (12) are integrated over each hemisphere to yield

$$\partial q^+ / (2\partial x) = -(\alpha + s) q^+ + s q^- + \alpha \sigma T_s^4 \tag{13}$$

$$-\partial q^- / (2\partial x) = -(\alpha + s) q^- + s q^+ + \alpha \sigma T_s^4 \tag{14}$$

At the interface 2, the absorptance of solid phase at temperature  $T_2$  for incident black radiation of reaction temperature  $T_m$  is equal to the emittance of surface at  $T_m$  for electrical non-conductors such as ceramics or metal oxide surfaces in which the monochromatic emittance is independent of temperature [20].

$$\text{At } x = x_2 : \quad q^- = E^* \sigma T_m^4 - E^* \sigma T_s^4 \tag{15}$$

Other boundary conditions are

$$\begin{aligned} x = 0 : \quad T_g &= T_i, \quad q^+ = 0, \quad d = d^* \\ x = x_2 - \Delta x : \quad T_g &\leq T_A, \quad d = 0 \\ \Delta x &\rightarrow 0 \\ x = x_2 : \quad y &= 0, \quad T_g = T_m, \quad d = 0 \\ x = x_3 : \quad y &= 1, \quad T_g = T_m \\ x = L : \quad T_g &= T_e, \quad q^- = 0 \end{aligned} \tag{16}$$

These equations are transformed into dimensionless form using following dimensionless quantities:

$$\begin{aligned} X^* &= x^* / L, \quad d' = d / d^*, \quad T^* = (T_g - T_i) / T_i, \\ M_1 &= \rho u c / (\sigma T_i^3), \quad M_2 = k_s / (\sigma T_i^3 L), \\ M_3 &= k_g / (\sigma T_i^3 L), \quad L^* = \alpha L \end{aligned} \tag{17}$$

The energy balance of the reaction region B is worked out by considering the total reaction heat release rate, sensible enthalpy flux of gas and radiative energy flux at both ends. The overall energy balance is made by equating the total reaction heat release rate to the sum of latent heat absorption loss, sensible enthalpy flux at downstream end, radiation heat losses at upstream and downstream ends. Heat conductive energy fluxes at both ends of porous medium are assumed to be negligible [3].

### 2.3. Numerical solutions

The governing differential equations with boundary conditions were numerically integrated using collocation method [21]. In this method the differential equations are converted to nonlinear system of equations with assumed polynomial spatial profiles for temperature and heat fluxes. These algebraic equations were solved using computer.

The computation was carried out using kerosene–air system in ceramic porous medium. Taking composition of kerosene as  $C_{12}H_{26}$ , the properties of  $C_{12}H_{26}$  as a function of temperature has been used [18]. The auto-ignition temperature of kerosene,  $T_A = 503$  K was used. For kerosene–air system, laminar burning velocity,  $u_L$  for stoichiometric oil–air mixture at 477 K is taken [22] as  $0.40 \text{ ms}^{-1}$ . The base line data are as follows:  $Q' = 1 \times 10^4$ ,  $T_i = 298$  K,  $f = 1.0$ ,  $L = 0.1$  m,  $\phi = 0.95$ ,  $c = 1.105 \text{ kJ kg}^{-1} \text{ K}^{-1}$ ,  $k_g = 0.078 \text{ W m}^{-1} \text{ K}^{-1}$ ,  $k_s = 0.18 \text{ W m}^{-1} \text{ K}^{-1}$ ,  $E^* = 0.3$ ,  $h_{gs} a_s = 2 \times 10^7 \text{ W m}^{-3} \text{ K}^{-1}$  as estimated [4].

### 3. Results and discussions

The temperature profiles as a function of  $X$ , inside the porous medium, at different optical thicknesses,  $L^*$  are shown in Fig. 2, with flame location  $X^* = 0.5$ . It may be mentioned that  $L^*$  ( $=\alpha L$ ) can be changed by varying the absorption coefficient of the porous medium,  $\alpha$  while  $L$  remains same at 0.1 m. For the same flame location,  $X^* = 0.5$ , the effects of  $L^*$  on the peak temperature,  $T^*$ , burning velocity,  $V^*$ , radiative efficiencies,  $E'$ ,  $E''$  and the optimum oil drop diameter,  $d^*$  are shown in Fig. 3. The temperatures of gas and solid coincide due to firstly, high value of  $h_{gs} a_s$  imposed [4,5] and secondly,

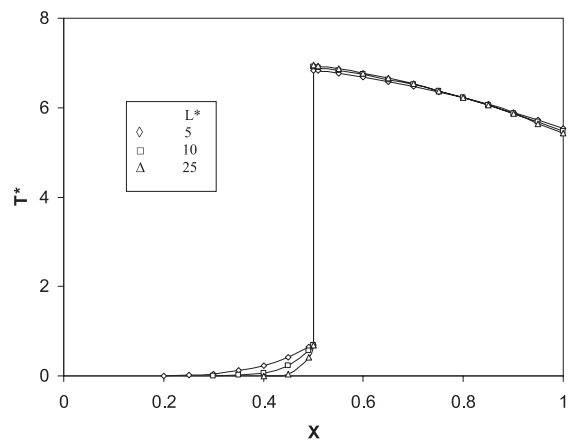


Fig. 2. Gas temperature profiles for several optical thicknesses when  $X^* = 0.5$ .

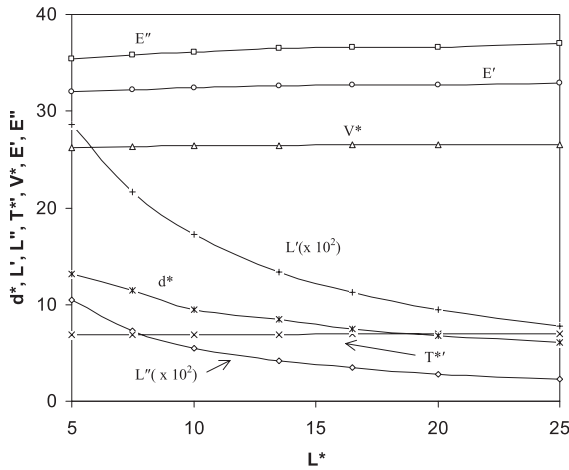


Fig. 3. Radiant output, peak gas temperature, burning velocity, preheating temperature zone length, oil vaporization length and optimum oil droplet diameter for varying optical thicknesses when  $X^* = 0.5$ .

negligible effect of small heat absorption rate for vaporization of liquid droplets in comparison to high value of radiative heat flux at any point in the preheating zone. With reaction peak temperature value,  $T^{*'}$  remaining above 2000K, the assumption of constant reaction temperature is satisfied. As  $L^*$  increases, the increased radiative energy feedback from the post flame region to reaction zone results in increase in  $V^*$ . Similar observations have been made earlier [3]. In Fig. 3, variation of  $L'$  and  $L''$  with  $L^*$  has been shown. Here  $L'$ , preheating temperature zone length,  $(x^* - x')/L$ , is defined arbitrarily as the dimensionless distance between  $x = x^*$  and  $x = x'$  where  $T^* = 0.01$  at  $x = x'$ . It has the physical meaning of  $T_g$  just starts increasing above  $T_i$  at  $x = x'$ .  $L''$ , effective oil vaporization length,  $(x^* - x'')/L$  is similarly defined as the dimensionless distance between  $x = x^*$  and  $x = x''$  where  $p_{v,o}/p$  becomes 0.01 at  $x = x''$ . It means at  $x = x''$ , the vaporization of oil just starts. For the present system, the value of  $T_g$  is nearly equal to 362K at  $x = x''$ . With increase in  $L^*$ , the preheating temperature zone length,  $L'$  and hence the effective oil vaporization length,  $L''$  shorten. So as  $L^*$  increases,  $d^*$  decreases. With increase in  $L^*$ , both downstream and upstream losses start increasing. This indicates that with increase in  $L^*$ , the radiative feedback increases from the post flame region towards upstream up to the air entry end. The oil droplet profile as a function of  $X$  at  $X^* = 0.5$  for different values of  $L^*$  are shown in Fig. 4. Sharp changes in  $d'$  occur due to sharp change in  $L'$  and  $L''$  with increase in  $L^*$  as observed in Fig. 3.

The radiative heat fluxes as a function of  $X$  in the porous media is presented in Fig. 5 when  $X^* = 0.5$ . Maximum radiative heat flux exchange occurs at the reaction zone  $X^* = 0.5$ . This supports the concept of radiative en-

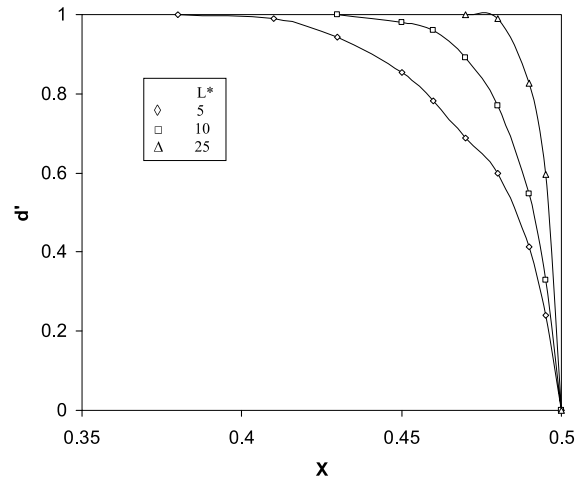


Fig. 4. Oil droplet profiles for different optical thicknesses when  $X^* = 0.5$ .

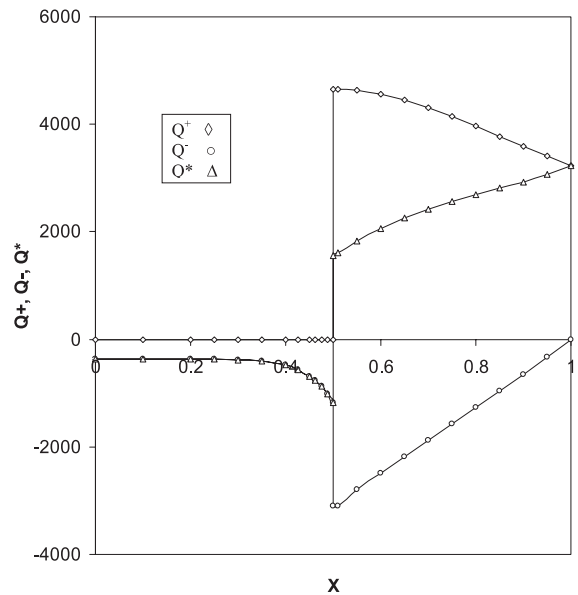


Fig. 5. Profiles in the radiant fluxes in the porous medium for  $L^* = 10$ ,  $X^* = 0.5$ .

ergy feedback in such systems proposed by Weinberg [23]. At the reaction zone, there are sharp changes in forward and backward heat fluxes. At both ends of the porous medium, the net heat fluxes represent heat losses. Similar observations were made by others [3,19].

Fig. 6 shows the effect of position of reaction zone,  $X^*$ , on gas temperature distribution. The reaction temperature and the temperature profile do not significantly change in the range of  $X^* = 0.2-0.8$  for  $L^* = 10$ . Variation of  $T^{*'}$ ,  $d^*$ ,  $V^*$ ,  $E'$  and  $E''$  with  $X^*$  is shown in

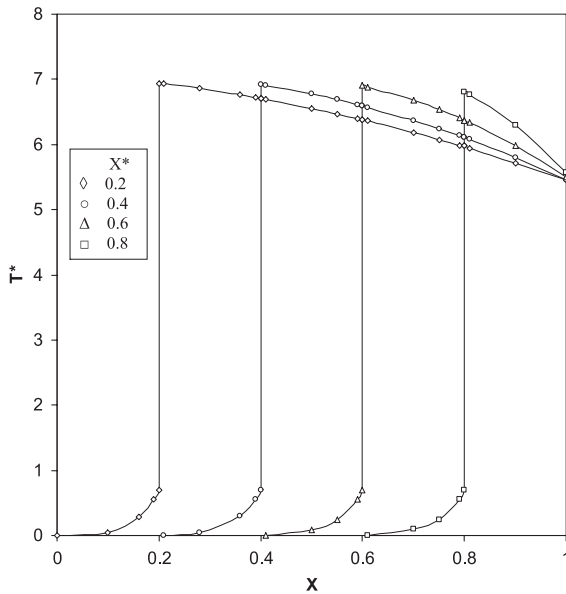


Fig. 6. Gas temperature profiles for several positions of the reaction zone for  $L^* = 10$ .

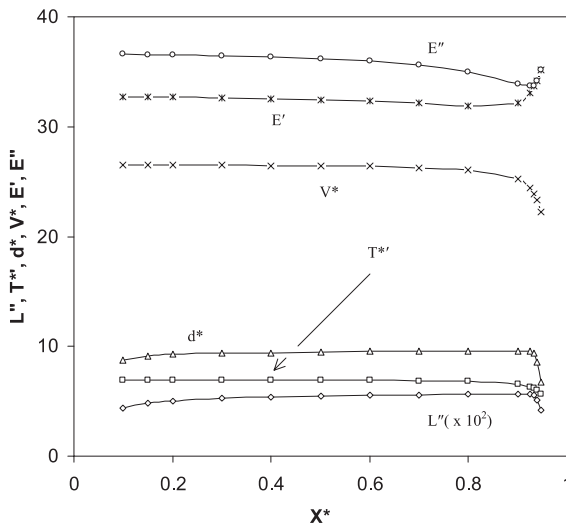


Fig. 7. Radiant output, peak gas temperature, burning velocity, oil vaporization length and optimum oil droplet diameter at several flame locations for  $L^* = 10$ .

Fig. 7 for  $L^* = 10$ . In Fig. 8 for various values of  $L^*$ , the effect of  $X^*$  on  $d^*$ ,  $L''$  is presented. In Fig. 7 with increase in  $X^*$  from 0.1 to 0.925,  $d^*$  and the oil vaporization length,  $L''$ , increase in a similar fashion. But at  $X^* > 0.925$  the sudden decrease in  $d^*$  occurs. This is firstly due to decrease in  $L''$  and secondly due to decrease in value of  $T_2$  from  $T_A$ . In other words, this is due to shorter vaporization length with lower preheat tempera-

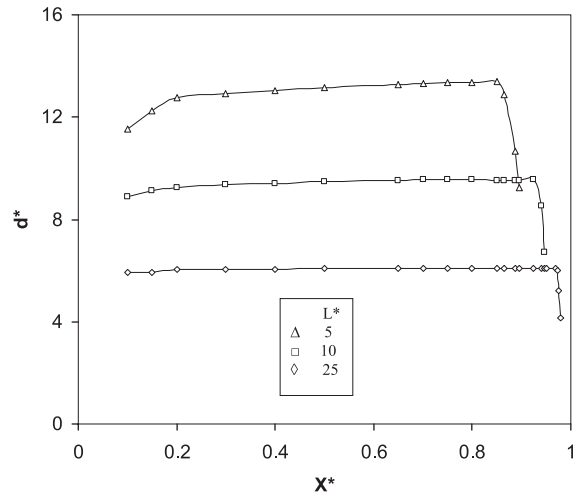


Fig. 8. Effects of position of reaction zone on optimum oil droplet diameter for several optical thicknesses.

ture profile as  $X^*$  increases from 0.925 to 0.947. In Fig. 8, variation of  $d^*$  with  $X^*$  is similar for  $L^* = 5, 10, 25$ . But as  $L^*$  is increased, early change of  $d^*$  at  $X^* < 0.2$  diminishes as well as highest value of  $d^*$ , which occurs at high values of  $X^*$ , decreases. In Fig. 7, the shifting of  $X^*$  towards the upstream end leads to the increase in upstream radiative end loss whereas the downstream loss is nearly constant for  $X^* < 0.9$ . With  $X^* > 0.925$ , the downstream loss starts increasing and upstream loss decreasing sharply and finally becomes zero with  $x^* \geq 0.93$ . In the porous medium, the radiative heat feedback depends on the value of  $T^{*'}$ ,  $V^*$  and effective upstream optical thickness. This affects  $T^{*'}$ ,  $V^*$  and the heat losses from both ends.

The effect of effective emissivity,  $E^*$  of the porous medium on its thermal performance is presented in Fig. 9. There is almost no change in  $T^{*'}$  and  $V^*$  with the variation in  $E^*$ .  $d^*$  remains constant with variation of  $E^*$  as the value of  $T_2$  remains at  $T_A$  throughout the range of  $E^*$ . As  $E^*$  increases, the radiative heat losses at the downstream and upstream ends decrease and increase respectively almost in a linear way. This indicates that the emissivity of material of construction of porous medium has a profound effect on thermal performance of system.

Fig. 10 shows the effect of reaction enthalpy flux,  $Q'$ , on the performance of the system.  $T^{*'}$  and  $V^*$  increase almost proportionately with  $Q'$ . The downstream loss,  $Q^*(L)$ , increases with  $Q'$ .  $E'$  and  $E''$  decrease sharply with increase in  $Q'$ . At low values of  $Q'$ , the radiative efficiencies are quite high. It shows that at low values of  $Q'$ , the conversion of sensible heat of gas to radiative heat becomes more efficient whereas at high values of  $Q'$ , the sensible heat loss in exit gas predominates over the radiative heat feedback. With increase in  $Q'$ ,  $d^*$

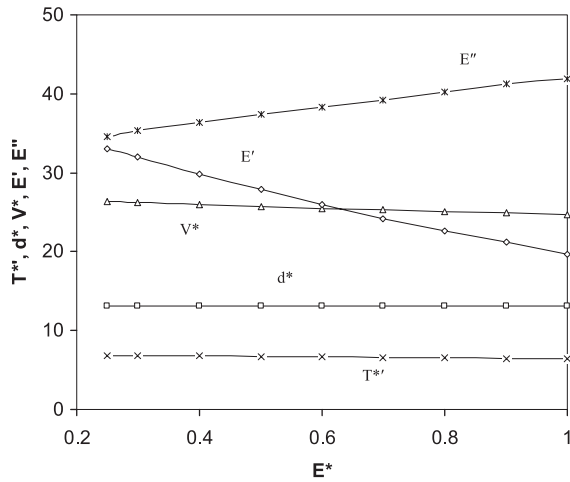


Fig. 9. Effect of emissivity of porous medium on radiative output, peak gas temperature, burning velocity and optimum oil droplet diameter for  $L^* = 5$  and  $X^* = 0.5$ .

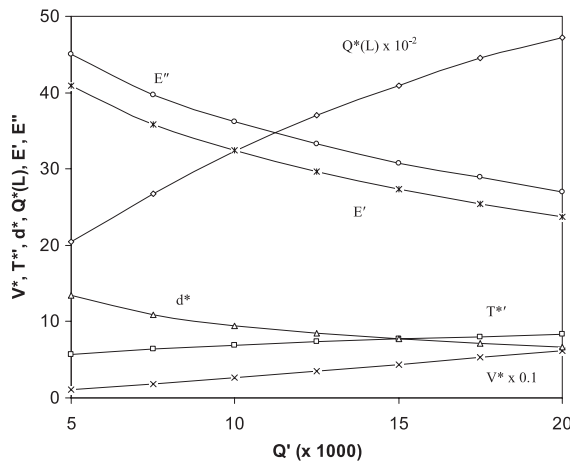


Fig. 10. Effect of reaction enthalpy flux on radiant output, peak gas temperature, burning velocity and optimum oil droplet diameter for  $L^* = 10$  and  $X^* = 0.5$ .

decreases due to the lower preheat temperature profile for high air flow rates.

It can be summarized that the optical thickness, flame position and emissivity play important role in determining the radiative end losses and optimum oil diameter. In an industrial application, the downstream radiative loss is used for thermal applications whereas the upstream radiative loss is undesirable because it is a waste of energy not suitable for safe handling of flammable gases. Also there is limitation in oil spray devices for the generation of fine oil droplets with low power input. The porous system which can handle large inlet droplet size and has high downstream radiative end loss

with no upstream loss is desirable. High downstream radiative loss without any upstream loss is obtainable with high values of  $X^*$  for combustion process. Large droplet diameter is obtained when the length of preheat temperature zone is large. This is obtained for low values of  $L^*$ . So the porous medium with low values of  $L^*$  (i.e. low absorption coefficient) with operating flame position more towards downstream end of the porous medium will be the desirable system for combustion of sprayed droplets suspended in air. It may be mentioned that energy consumption for oil breakup to large droplets will be much less in comparison to that required for small droplets.

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